

Patent Application

OPTICAL BANDWIDTH METER FOR LASER LIGHT

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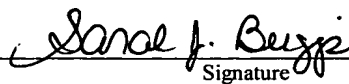
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TITLE

Optical Bandwidth Meter for Laser Light

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RELATED APPLICATION

This application is related to an application entitled METHOD AND APPARATUS FOR MEASURING BANDWIDTH OF AN OPTICAL OUTPUT OF A LASER assigned to the assignee of the present application and previously filed (Attorney Docket No. 2003-0056-01), the disclosure of which is hereby
15 incorporated by reference.

FIELD OF THE INVENTION

The present invention relates to the determination of the spectral bandwidth of a laser. More generally the present invention relates to the accurate estimation of
20 the bandwidth of an optical source using interferometric or dispersive instruments (“spectrometers”) whose impulse response functions have bandwidth generally comparable to or larger than that of the source being measured.

BACKGROUND OF THE INVENTION

25 Spectrometers based on dispersive optical elements or optical interference phenomena are well-known instruments commonly applied for the measurement of the absolute wavelength and bandwidth of light sources. When employed as a bandwidth-measuring tool (“bandwidth meter”), the effect of the finite impulse response of the spectrometer must be considered when determining the actual
30 bandwidth of the source being measured. For the purpose of the present application, “bandwidth” may refer to any number of metrics or mathematical constructions related to the details of the optical source spectrum, such as full-width of the

spectrum at half-maximum peak intensity (FWHM), full-width at some percentage “X” of the peak intensity (FWXM), width of the 95%-enclosed energy integral about the peak (I95% or E95%), etc. An accurate knowledge of the bandwidth of an optical source is very important for many scientific and industrial applications, for example in spectroscopy of liquids and gases, critical dimension control in deep-ultraviolet (DUV) semiconductor photolithography, etc.

In very simple cases, for example when the spectrum of the source and the spectrometer impulse response are accurately represented both by purely Gaussian or both by purely Lorentzian functions, the effect of the spectrometer impulse response can easily be accounted for using simple algebraic equations for many bandwidth metrics. The output spectra of most optical sources, e.g., lasers, do not have such simple forms in general and may change with time or operating condition. Further, the impulse response of the spectrometer may be similarly complex or unknown.

A common method employed to surmount these obstacles is to employ a spectrometer whose impulse response has a bandwidth so narrow in comparison to the expected bandwidth of the source to be measured that its influence is negligible. That is, the spectrometer impulse response is well-approximated by a mathematical delta-function for the case in question. However, it is not always practical or even possible to obtain a spectrometer with such a narrow-bandwidth impulse response, particularly when it is required to be very narrow in comparison to a source such as a laser which itself may be extremely narrow (tens of femtometers or less on a wavelength scale).

A second and somewhat more sophisticated method commonly used approximates the spectrometer impulse response function and the source spectrum with analytic functions (e.g., of Lorentzian, Gaussian, or mixed type) for which the effects of convolution within the spectrometer can be calculated beforehand and then expressed in simple mathematical terms. As noted above, this is not necessarily a good approximation, and can fail or become very difficult to implement dependably for certain types of bandwidth metrics. Calculation of integral bandwidth metrics

such as E95% can be inaccurate or very computationally intensive using this technique.

As an illustration of second method and its shortcomings, consider a recently released product of Cymer, Inc., the owner by assignment of the present application.

5 This product, the XLA-100, contains an onboard bandwidth meter employing a single etalon with a FWHM bandpass of about 0.12 pico-meter (pm) that is used to interrogate the output of a deep-ultraviolet excimer laser light source having an average typical FWHM bandwidth of about 0.17 pm. The above approximation is made in which both the laser and the etalon spectrometer are assumed to have an
10 analytic Lorentzian spectral shape; therefore, the FWHM of the etalon spectrometer fringe is found mathematically to be simply the sum of the FWHMs of the laser source and the etalon spectrometer impulse response. In this Lorentzian approximation, then, the actual laser source bandwidth is estimated by the FWHM of the etalon spectrometer fringe, minus the FWHM of the etalon spectrometer
15 impulse response (determined in independent measurements). However, because the ratio of the FWHM bandwidths of the source spectrum and impulse response function is close to unity, this method may lose accuracy in the event that the shape of the laser spectrum deviates too far from an approximately-Lorentzian shape. For example, a narrowing of the central spectral peak of the source spectrum with a
20 concomitant increase in energy in the near wings can result in an over-estimation of the FWHM bandwidth in this approximation.

If the detailed shape of the laser spectrum is constant, the offset subtracted in this example can sometimes be adjusted to compensate. However, if the shape of the laser spectrum changes with operating conditions, with system alignment, or
25 over the lifetime of the product, even this compensation will not remain accurate. Also at issues is the complicating possibility that in a manufacturing setting, the etalon spectrometer may be tested and offset-calibrated on one laser, but is ultimately be installed on another that has a slightly different spectral shape. In this case the calibration may be in error.

30 It is the purpose of this invention to mitigate these and similar measurement errors by employing more than one spectrometer operating in parallel within a single

bandwidth meter, where the multiple spectrometer sub-circuits have significantly different impulse response function bandwidths. Because each sub-circuit has a different bandpass, each sub-circuit has a correspondingly different relative sensitivity to energy content in various regions of the spectrum. For example, a fringe FWHM measurement of the output of a very narrow bandpass circuit will give a result that accurately approximates the FWHM of the source spectrum, but a fringe FWHM measurement of a very wide bandpass circuit will give a result that is more closely related to the total energy content of the source spectrum. By choosing the bandwidth of the impulse response functions of the sub-circuits carefully, it is possible to mitigate the errors described above and simultaneously provide accurate estimates of integral bandwidth metrics such as the E95 width using only simple algebraic equations. A significant advantage of the invention is that these simple equations can be handled with little computational overhead, important for real-time applications such as bandwidth monitoring or sensing in high-repetition-rate pulsed lasers.

SUMMARY OF THE INVENTION

A method and apparatus for measuring bandwidth of light emitted from a source is disclosed which may comprise: first and second wavelength sensitive optical bandwidth measuring devices (“spectrometers”), these spectrometers having differing impulse response functions, and each providing, respectively, an output representative of a measured parameter related to, or containing information about the bandwidth of the source as measured respectively by the first and second spectrometers, and an actual bandwidth calculation apparatus adapted to utilize these two outputs as part of a multivariable equation or system of equations employing predetermined calibration variables specific to both the first and the second spectrometers, used to calculate an estimate of the source bandwidth according to one metric and a second estimate of the source bandwidth according to a different metric. The source bandwidth metric may be a spectrum full-width at some percentage of the maximum value attained (“FWXM”), and the second source bandwidth metric may be the width of a portion containing some percentage or

fraction of the total energy ("EX"). The first and second spectrometers may be etalon spectrometers and the measured output parameters may be representative of an etalon fringe width as measured by a position-sensitive photodetector. The precomputed modeling variables and equations may be determined via an empirical measurement in which the behavior of the measured output parameters provided by the two spectrometers are compared with the values of two bandwidth metrics from a simultaneous known-accurate measurement of the actual source spectrum, which may be FWXM and EX. The response of the two spectrometers to interrogation of the known source spectrum may be mathematically modeled as dependent variables using this information, using a set of simultaneous linear equations or some other simple relation. The coefficients of the linear equations or other mathematical model may be determined by least-squares fitting of the model to the dependent variable data, in response to the independent variables provided by the known-accurate source bandwidth metrics. In the case of the simultaneous linear equation model, there will result from this procedure two equations in two unknowns that model the spectrometer measured output parameters: (first, second spectrometer output parameter) = (A,D * (calibrating source spectrum known value of FWXM)) + (B,E* (calibrating source spectrum known value of EX) +C,F. The model may be inverted to estimate the bandwidth of the source spectrum: (estimate of first source bandwidth parameter) = ((B * (second spectrometer output)) – (E * (first spectrometer output)) + CE – BF) / (BD – AE), or the equation: (estimate of second source bandwidth parameter) = ((A * (second output)) – (D * (first output)) + CD – AF) / (AE – BD). FWXM may be FWHM and EX may be E95. The impulse response function of the first spectrometer may be selected to be much more sensitive to FWXM than to EX and the impulse response function of the second spectrometer may be selected to be much more sensitive to EX than to FWXM.

BRIEF DESCRIPTION OF THE DRAWINGS

Fig. 1 shows a representative example of a three dimensional plot of the response of an etalon spectrometer of the prior art to laser light varying by known

amounts in FWHM and E95, as measured by a calibrating source of laser light which is relatively adjustable in FWHM and E95;

Fig. 2 shows a representative plot of the type shown in Fig. 1 for a bandwidth meter according to the present invention having, e.g., an etalon that is relatively more sensitive to change in FWHM than to change in E95;

Fig. 3 shows a representative plot of the type shown in Fig. 1 for a bandwidth meter according to the present invention having, e.g., an etalon that is relatively more sensitive to change in E95 than to FWHM compared to the first;

Fig. 4, there is shown a schematic block diagram of a bandwidth meter according to an embodiment of the present invention.

Fig. 5 shows a plot indicating the superior estimation of actual source FWHM bandwidth utilizing the present invention;

Fig. 6 shows the reduction in the error utilizing the present invention;

Fig. 7 illustrates the estimation of E95 utilizing a bandwidth meter made according to an embodiment of the present invention;

Fig. 8 illustrates the reduction in error of a simulated bandwidth meter made according to an embodiment of the present invention.

DETAILED DESCRIPTION OF PREFERRED EMBODIMENTS

Turning now to Fig. 1 there is shown a three-dimensional plot of the response of a bandwidth meter employing, e.g., an etalon spectrometer, e.g., an etalon manufactured by Coherent, Inc., as the values of FWHM and E95 are varied as measured utilizing a very accurate spectrometer, e.g., a grating spectrometer, e.g. ELIAS-I as manufactured by Laser Technik Berlin ("LTB").

It can be seen that the etalon spectrometer response is comparably influenced by changes in both E95 and to FWHM of the source (a line-narrowed discharge-pumped excimer laser) over the operating range. All units are in picometers. A least-squares fit to a plane model of the data yields the approximation (etalon fringe width) = $A \cdot (\text{source FWHM}) + B \cdot (\text{source E95}) + C$ with $A = 0.64495 \pm 0.0166$, and $B = 0.20797 \pm 0.01105$ and $C = 0.22983 \pm 0.00719$. In the prior art this response has been modeled in a simpler form, in some cases where A is set

identically equal to one and B is set identically equal to zero, and all of the modeling is done by adjusting the constant offset term C during calibration. In the prior art the response has also been modeled by a linear equation where the B term is set identically equal to zero so that the model takes a linear form, with the slope A and intercept C chosen to most accurately model the response as measured during the calibration process. Because the term modeling the E95 response is not entirely orthogonal to the term modeling the FWHM response, this latter method works better than that using the constant offset alone. A feature of the present invention is the ability to incorporate all three terms, which yields still better performance (but requires more than one spectrometer sub-system to fully determine the inputs to the equations).

Turning now to Fig. 2 there is shown a three dimensional plot of a simulated spectrometer, e.g., an optical bandwidth measuring device, e.g., an etalon spectrometer, which, e.g., determines the bandwidth of the input laser light by measuring the FWHM of a fringe created by the etalon projected optically onto a position-sensitive photodetector, e.g., a collection of photo-diodes arranged in a linear array (photo-diode array or "PDA"). The FWHM of the simulated spectrometer's impulse response is 0.12 pm, and the position-sensitive detector is simulated to approximate the prior art as implemented in released products of the assignee of this disclosure. The observed response indicates that the bandwidth meter is more sensitive to change in the FWHM than to a change in the E95 of the input spectrum for the spectral shape changes expected from a line-narrowed excimer laser. A least-squares fit of the data shown in Fig. 2 to the plane model results in the parameters $A = 0.66704 \pm 0.00221$ and $B = 0.8951 \pm 0.00079$ and $C = 0.10172 \pm 0.00039$.

Turning now to Fig. 3 there is shown a three dimensional plot of a second simulated spectrometer, e.g., an optical bandwidth measuring device, e.g., an etalon spectrometer, which, e.g., determines the bandwidth of the input laser light by measuring the FWHM of a fringe created by the etalon projected optically onto a position-sensitive photodetector, e.g., a collection of photo-diodes arranged in a linear array (photo-diode array or "PDA"). The FWHM of the second simulated

spectrometer's impulse response is 0.70 pm, and the position-sensitive detector is also simulated to approximate the prior art. The response indicates that the bandwidth meter is relatively more sensitive to change in E95 than to FWHM, when compared to the first simulated spectrometer. A least-squares fit of the data shown
5 in Fig. 3 to a plane model results in the parameters $D = 0.14483 \pm 0.00114$ and $E = 0.16575 \pm 0.00041$ and $F = 0.67263 \pm 0.0002$.

Applicant has discovered that such a set of observations for each of two different bandwidth meters having differing impulse response functions, demonstrates that one spectrometer will be more sensitive to change in FWHM of
10 the input spectrum and the other will be relatively more sensitive to change in E95 of the input spectrum. The differing impulse response can be provided by various means, e.g., by employing etalon spectrometers each having different finesse or the same finesse and different free-spectral ranges, or some combination thereof. The applicant has discovered that the spectral shape variations commonly encountered in
15 line-narrowed discharge-pumped excimer lasers are adequately modeled by plane equations as described above; that is, modeled by two separate linear equations (one for each spectrometer) as follows:

(first output, e.g., value related to the fringe width of etalon spectrometer 1)
= $(A * (\text{known actual value of the full width at some percent of the peak of the}$
20 $\text{source spectrum, e.g., FWXM})) + (B * (\text{known actual value of the width between}$
 $\text{two points about the peak of the actual source spectrum containing some percentage}$
 $\text{of the energy of the total source spectrum, e.g., EX}) + C$; and

(second output, e.g., value related to the fringe width of etalon spectrometer
2) = $(C * (\text{known actual value of the full width at some percent of the peak of the}$
25 $\text{source spectrum, e.g., FWXM})) + (D * (\text{known actual value of the width between}$
 $\text{two points about the peak of the source spectrum containing some percentage of the}$
 $\text{energy of the total source spectrum, e.g., EX}) + E$.

Given this information the bandwidth calculation apparatus can be programmed to invert the models and obtain an estimate of the source bandwidth
30 parameters using the derived equations:

(estimate of the first source bandwidth parameter, e.g., estimate of the actual source FWXM) = $((B * (\text{second output, e.g., etalon 2 fringe width})) - (E * (\text{first output, e.g., etalon 1 fringe width})) + CE - BF) / (BD - AE)$,
or the equation:

5 (estimate of the second source bandwidth parameter, e.g., estimate of the actual source EX) = $((A * (\text{second output, e.g., etalon 2 fringe width})) - (D * (\text{first output, e.g., etalon 1 fringe width})) + CD - AF) / (AE - BD)$.

In the more specific case where FWXM is the FWHM value of the source spectrum and EX is the E95 width of the source spectrum, and X is the width of the
10 fringe imaged on the first etalon spectrometer PDA and X' is the width of the fringe imaged on the second etalon spectrometer PDA, then the fringe widths may be modeled by the two equations $X = A*FWHM + B*E95 + C$ and $X' = D*FWHM + E*E95 + F$ in accordance with the preceding description. Therefore, the model may be inverted to obtain the following estimates of the source bandwidth:

15 $FWHM = (B*X' - E*X + CE - BF) / (BD - AE)$, and
 $E95 = (A*X' - D*X + CD - AF) / (AE - BD)$.

According to this invention the two spectrometers are combined into a single bandwidth-meter, e.g., to operate in parallel, and the controller, discussed below, can be programmed to utilize the two outputs of the component spectrometers with the
20 previously determined calibration values for each bandwidth meter, e.g., A through F, to solve for either or both of FWXM and EX. That is, full width at some percent of the maximum, e.g., FWHM or FW75%M, and/or EX, i.e., the width of the spectrum about the peak within which some percentage of the total energy is contained, e.g., E95% ("E95") or E97% or E93% etc., can be solved for by storing
25 the respective coefficients in memory available to the processor and by providing to the processor actual outputs from the respective component spectrometers. It will be understood that if metrics other than the source FWHM and/or source E95 are to be measured and calibrated for at the factory, then such other value(s) will be the ones against which the output, e.g., etalon fringe measurement, will be modeled as
30 discussed above to derive the model parameters, e.g., coefficients A through F above.

Turning now to Fig. 4, there is shown a schematic block diagram of a bandwidth meter 10 according to an embodiment of the present invention. The bandwidth meter 10 may be set up to measure the bandwidth of a light beam 14 produced by a source such as a laser, e.g., a discharge-pumped line-narrowed excimer laser, or excimer laser plus power amplifier or power oscillator. The output of the source may be split, e.g., in a beam splitter 16 which can be set to pass most of the beam 14 and reflect a small portion in beam 18 which can pass through a second beam splitter 20 which may be set to reflect and pass essentially identical amounts of the beam 18 in a reflected beam 22 and a passed beam 24, each of which enter a respective spectrometer 30, 34. The spectrometers 30, 34 may comprise a bandwidth-sensitive measuring apparatus, e.g., they may include etalons for creating fringes the width of which are indicative of the bandwidth of the light measured and electrical circuits (not shown) for sensing the spectrometer fringes and providing an analog or digital input to a controller 40 which may be representative of the measurement. The etalon 30 may, e.g., be selected to have nominal bandpass values of, e.g., 0.12 pm FWHM, a free spectral range of, e.g., 3pm at 193.36nm, for an ArF laser bandwidth measurement, e.g., over a 10mm aperture, and a peak transmission (ratio of the fringe peak photo-electrical signal and the input peak signal) of $\geq 50\%$ at 193.350 nm normal incidence. The etalon 34 may be selected to have nominal bandpass values of, e.g., 0.7 pm FWHM a free spectral range of, e.g., 20 pm at 193.36, for an ArF laser bandwidth measurement, e.g., over a _mm aperture, and a peak transmission (ratio of the fringe peak photo-electrical signal and the input peak signal) of \geq _% at 193.350 nm normal incidence.

The bandwidth monitoring capability afforded by the present invention may assist in the application of the laser light beam 14, as an illuminating source for, e.g., exposing photoresist through a reticle (mask work) using projection optics with refracting components in sub-micron fabrication of integrated circuits, micromachines, nano-technologies, or the like ("photolithography").

It will be understood that this type of calibration can be employed with other bandwidth measurement instruments that are susceptible to the same or similar kinds of frequency dependent response issues.

It will be understood from the above that applicant has created an optical bandwidth measuring apparatus based upon parallel simultaneous measurements of an optical source, e.g., output from a laser, by utilizing the characteristics of two spectrometers with different impulse response functions. The two arms of the bandwidth measuring apparatus exhibit differential sensitivity to the energy content in different regions of the spectrum, and when combined with a simple but appropriate mathematical model can be used to estimate the source bandwidth more accurately than the prior art in the presence of spectral shape changes. The output of each of the two parallel bandwidth measuring sub-systems, e.g., the FWHM values of fringes created by each respective etalon spectrometer provide inputs to a system of simultaneous linear equations that can be used to find a good approximation of the actual FWHM and E95% widths of the laser light being measured.

Data taken for the measurements and simulations illustrated, e.g., in Figs. 1 – 3 are provided by measurement of the FWHM and E95 widths of a set of source spectra from 193 nm line-narrowed ArF excimer lasers using high-resolution double-pass grating spectrometers manufactured by Laser Technik Berlin, while simultaneously determining the width of several etalon spectrometer fringes in response to the source spectrum inputs. The grating spectrometers were independently calibrated with a solid-state 193 nm source narrower in bandwidth than the grating spectrometer impulse response, this itself being independently verified with a high-finesse etalon. Plots of a real etalon spectrometer response to the FWHM and E95 width variations of NL-7000 single-oscillator laser spectra (Fig 1) and response of simulated etalon spectrometers to actual spectra from XLA-100 master-oscillator power-amplifier configurations (Figs 2-3). The NL-7000 and XLA-100 are products of the assignee of the present application. From these plots the applicant discovered that the behavior of the output of an etalon spectrometer could be reasonably approximated by a plane surface, and therefore modeled using only three free parameters over the given range of source spectrum variations. The applicant also discovered from this data that the parameters in the model are sensitive to the bandwidth of the impulse response (bandpass) of the spectrometer employed. From this behavior the applicant devised the invention disclosed herein,

by concluding that two such spectrometers could be employed simultaneously, and the differing response used to extract more information about the source spectrum than available using the prior art. In particular, the model is sufficiently accurate and easily inverted and as such can be employed to estimate the FWHM and E95 width of a source spectrum over a reasonable range of spectral shape variations as are commonly encountered with line-narrowed excimer lasers when properly calibrated.

According to the disclosed embodiment of the present invention the accuracy of on-board bandwidth metrology for lasers and other sources, e.g., spectral FWHM can be improved significantly and other metrics such as E95 width can be incorporated simultaneously. The choice of a particular metric as optimal for certain applications like delivering very spectrally pure light for photolithography is still under debate; however this method appears to be flexible enough to accommodate many different choices. In addition the optimal selection of, e.g., the difference in the bandpasses of the two etalon spectrometer sub-systems remains to be determined, as does the exact functional form of the model. As discussed below this can be determined empirically by comparing the response of the spectrometer to the actual variations in the source spectrum, and choosing the model and parameters accordingly to optimize performance, e.g., accuracy and ease of implementation.

Turning now to Fig. 5 there is shown an illustration of the FWHM tracking capabilities of a simulated bandwidth-meter according to an embodiment of the present invention. Turning now to Fig. 6 there is shown an illustration of the FWHM tracking error (i.e., the discrepancy between the actual source spectrum FWHM and the FWHM reported by the bandwidth meter), showing a much narrower variance around a mean much closer to zero and the avoidance of discrepancies lying outside the expected statistical distribution. Large outliers represent a significant performance risk for modern bandwidth reporting systems. Turning now to Fig. 7 there is shown an illustration of the E95% tracking error of a simulated bandwidth detection apparatus according to the present invention. Turning now to Fig. 8 there is shown an illustration of E95 tracking error for the

simulated bandwidth detection apparatus according to the present invention,
measured in the tens of femto-meters.

The apparatus and method according to the described embodiment of the
present invention provides overall improved predicted and actual tracking (e.g., ~ a
5 factor of 2 reduction in FWHM error variance) and reduces the incidence of outliers
in tracking error, e.g., due to actual E95 changes in the measured light beam. The
present invention also gives greatly improved portability of coefficients between
calibration and operation under different conditions, e.g., variations in laser medium
enrichment and manufacturing spectral variability. It also appears to offer more
10 accurate on-board E95 tracking (e.g., $\pm 0.015\text{pm}$) utilizing robust technology, e.g.,
etalons in parallel. This E95 tracking can be expected to improve over the prior art,
e.g., which uses only a single etalon-spectrometer to estimate the source E95 width.

Those skilled in the art will appreciate that an aspect of the disclosed
embodiment of the present invention is that the method and apparatus may be
15 applied to calibrate the bandwidth-meter to provide a calculated output indicative of
a particular source bandwidth metric, e.g., EX, where the measured metric is not of
the same type, i.e., it could be the FWXM of the spectrometer fringe that is
measured, which may be easier to more accurately detect and/or more
computationally simple to compute from observable information.

20 It will also be recognized that the bandwidth metrics chosen for reporting
and for input to the model may be chosen from a whole host of types, not all of
which are listed herein. Those skilled in the art will understand that as a
generalization of an embodiment of the present invention, Z_1 can be considered to be
related to the source bandwidth as measured by one spectrometer and Z_2 can be
25 considered to be related to the source bandwidth as measured by a second
spectrometer acting in parallel. Also BW_1 can be considered to be a bandwidth
measure of the source, e.g., the output of an excimer laser, that is desired to be
known, and BW_2 can be a second such bandwidth measure of the source that is
desired to be known. According to an embodiment of the present invention then,
30 either BW_1 or BW_2 or both may be calculated from the outputs Z_1 and Z_2 of the
parallel spectrometer sub-systems and a model having predetermined coefficients as

described above, provided that models for the behavior of the individual spectrometer sub-systems in response to changes in BW_1 and BW_2 is chosen appropriately and can be simultaneously inverted to solve for the desired quantities.

It will also be understood that the “actual” source bandwidth cannot be
5 precisely measured without access to a spectrometer with resolving power greatly exceeding the actual bandwidth of the source. Even perfect calibration constant coefficients according to an embodiment of the present invention would have at least the error inherent in the calibrating spectrometer measurement, which may be small, but still finite—plus the error in the approximating model. The applicant estimates
10 such error to be in the femto-meter range for spectral shape changes in line-narrowed excimer lasers the applicant has observed. Therefore the terms “source bandwidth” and “actual source bandwidth” used in the specification and claims refer to the bandwidth measured by a suitably accurate calibrating instrument, grating spectrometer or otherwise. Similarly, the estimated “source bandwidth” as reported
15 by the invention disclosed herein is not the actual source bandwidth, but an estimate is much closer to what the suitably accurate calibrating instrument would report than would be expected from prior art bandwidth-meters. This is especially true in the presence of spectral shape changes incurred during normal operation of excimer lasers which may pronouncedly interfere with the ability of existing bandwidth-
20 meters to report the source bandwidth with the required degree of confidence.

Those skilled in the art will appreciate that the apparatus and methods of the present invention includes mathematical approximations and calibration methods that make the apparatus simple to implement using straightforward mathematics, and does not require detailed knowledge of the spectral shape of the input source or
25 impulse response functions of the spectrometer(s). Those skilled in the art will also appreciate that a feature of the described embodiment of the present invention is that it is relatively computationally simple, involving simple mathematical operations.

The above-described embodiments of the present invention are intended only for explanation and illustration purposes and are not the only embodiments in which
30 the present invention may reside. Those skilled in the art will understand that many modifications and changes may be made to the described embodiments without

changing the intent and spirit of the present invention. For example, other wavelength-discriminating apparatus (spectrometers) besides etalon spectrometers may be utilized to provide the parallel bandwidth measurements and calibrations. A wide range of bandpass values or differing impulse response functions for the two
5 parallel bandwidth detectors may be utilized and certain ranges and/or combinations may prove better for different applications, varying requirements for wavelength, bandwidth, etc. In addition, while the present invention has been explained with an embodiment utilizing two etalon spectrometers and two plane models, it may be possible to implement the invention utilizing, e.g., more than two
10 etalons/spectrometers instead of two, and/or possibly some other kind of modeling different from the plane $z = Ax + By + C$ (e.g., other relatively simple surfaces, e.g., a parabolic surface, depending on what the spectral variations in the source are expected to be what kind of spectrometers are used). The scope of the present invention, therefore, should be considered in light only of the appended claims and
15 legal equivalents.